

# Odds Chen Type Generated Family of Distributions

## Abstract

Inspired by [1] and [2] we introduce the odds Chen type generated family of distributions, and show a sub-model of this broad class of statistical distributions is a good fit to real-life data. Our hope is that readers will consider investigating some properties and applications of this new class of distributions.

## Keywords:

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1. The New Family Illustrated

### 1. The New Family Illustrated

We begin with the following

**Definition 1.1:** Let T be a random variable with PDF  $g(t)$  and CDF  $G(t)$ , and let X be a random variable with CDF  $F(x)$ , the odds Chen generated family of distributions (“Odds CT-X” for short) is defined by the following integral for its CDF

$$\int_0^{\frac{F(x)}{1-F(x)}} \frac{\lambda \beta}{1 - e^{-\lambda(1-e)}} g(t) G(t)^{\beta-1} e^{G(t)^\beta} e^{\lambda(1-e)G(t)^\beta} dt$$

where  $\lambda, \beta > 0$

From the above we have the following

**Proposition 1.2.** The CDF of Odds CT – X is given by

$$\frac{\lambda \left( 1 - e^{-G\left(\frac{F(x)}{1-F(x)}\right)^\beta} \right)}{1 - e^{-\lambda(1-e)}}$$

where the random variable T has CDF G, the random variable X has CDF F(x), and  $\lambda, \beta > 0$ , and  $x \in \text{Supp}(F)$

For illustrative purposes, let us assume  $T \sim \text{Exponential}(f)$ , and  $X \sim \text{Normal}(c, d)$ , then from the Proposition immediately above we have the following

**Theorem 1.3.** The CDF of Odds Chen Exponential-Normal is given by

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## Short Communication

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Submission: March 30, 2020

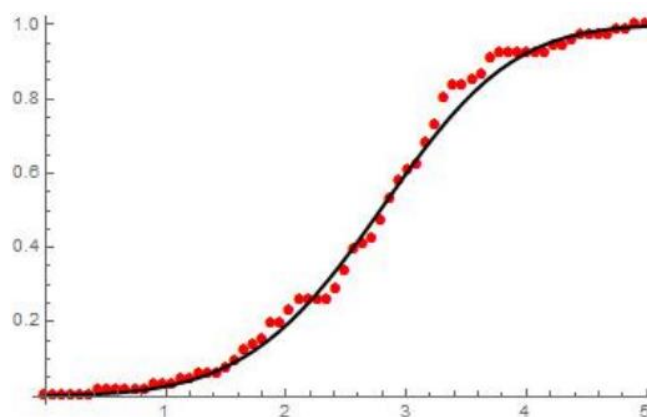
Published: April 13, 2020

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$$\frac{1 - \exp \left( \lambda \left( 1 - \exp \left( \left( 1 - \exp \left( -\frac{f \operatorname{erfc} \left( \frac{c-x}{\sqrt{2}d} \right)}{2 \left( 1 - \frac{1}{2} \operatorname{erfc} \left( \frac{c-x}{\sqrt{2}d} \right) \right) \right)^\beta \right) \right) \right)}{1 - e^{-(1-e)\lambda}}$$

where  $\operatorname{erfc}(\cdot)$  gives the complementary error function,  $d, f, \lambda, \beta > 0$ , and  $x, c \in \mathbb{R}$ .

Obviously, the PDF can be obtained upon differentiating the CDF above. We write  $W \sim \text{OCEN}(\lambda, \beta, f, c, d)$ , if W is an Odds Chen Exponential-Normal random variable. The Odds Chen Exponential Normal distribution is a good fit to real life data as shown Below



**Figure 1:** The CDF of OCEN (0.298716, 5.67999, 9.68395, 5.52968, 3.18486) fitted to the empirical distribution of Table 2 [3]

## References

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